

Workshop for Computational Techniques for Sustainability and
Resilience, Ishigaki, Okinawa

**Overview of the benefits of logic programming
to check dynamics properties in the Process
Hitting framework**

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Context and Aims

MeForBio team:
Algebraic modelling to study
complex dynamical biological systems

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1) What are the models?

Biological Regulatory Networks (BRNs): Studying **gene interactions** with mathematical tools;
Process Hitting (PH): a new developed model.

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Predicting the **evolutions** of the network.

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3) What for?

Searching of PH **properties** through ASP (fixed points, reachability).

Plan

- 1) Answer set programming (ASP)
 - Definition
 - Example of an ASP program

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- 4) Towards the model-checking of timed models through ASP
- 5) Conclusion & prospect

Answer Set Programming

ASP:

- Logic program written in language of AnsProlog*
- Form of rules :

$$\begin{array}{l}
 \textit{head} \leftarrow \textit{body}. \\
 L_0 \leftarrow L_1, \dots, L_m, \textbf{not } L_{m+1}, \dots, \textbf{not } L_n.
 \end{array}$$

with each L_j : literal in the sense of classical logic.

Rule's meaning:

If L_1, \dots, L_m are **true** and if L_{m+1}, \dots, L_n are **false**
then L_0 is **true**.

Answer Set Programming

Special types of rules:

- **Constraint** :

$$\leftarrow L_1, \dots, L_m, \text{ not } L_{m+1}, \dots, \text{ not } L_n.$$

- **Fact** :

$$L_0.$$

- **Cardinality** :

$$\min\{L_0, \dots, L_j\} \max \leftarrow L_1, \dots, L_m, \text{ not } L_{m+1}, \dots, \text{ not } L_n.$$

Answer Set Programming

Example:

A clique in a graph is a set of pairwise adjacent vertices.

```
vertex(1..99). % 1,...,99 are vertices
```

```
edge(3,7). % 3 is adjacent to 7
```

```
...
```

```
edge(X, Y) : -edge(Y, X), vertex(X; Y).
```

```
% GENERATE
```

```
5{in(X) : vertex(X)}.
```

```
% TEST
```

```
: -in(X), in(Y), vertex(X), vertex(Y), X! = Y, not edge(X, Y).
```

The Process Hitting modeling



Sorts: components a, b, z

The Process Hitting modeling



Sorts: components a, b, z

Processes: local states / levels of expression z_0, z_1, z_2

The Process Hitting modeling

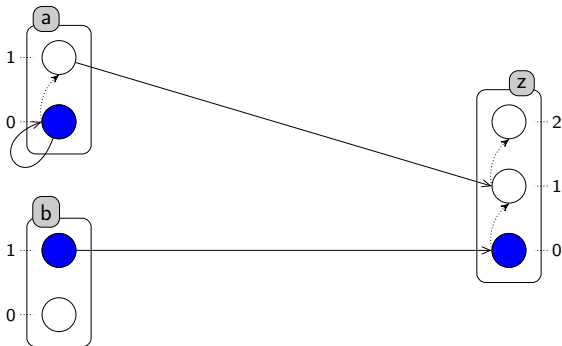


Sorts: components a, b, z

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States: sets of active processes $\langle a_0, b_1, z_0 \rangle$

The Process Hitting modeling



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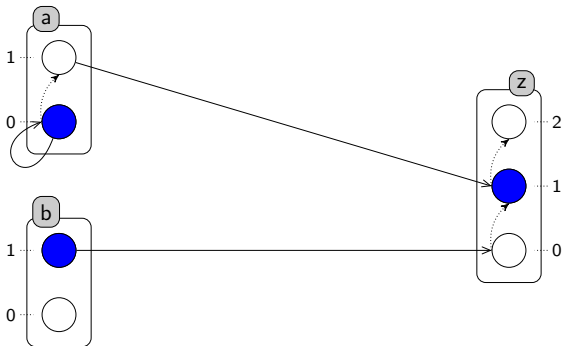
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Actions: dynamics $b_1 \rightarrow z_0 \dot{\rightarrow} z_1, a_0 \rightarrow a_0 \dot{\rightarrow} a_1, a_1 \rightarrow z_1 \dot{\rightarrow} z_2$

$b_1 \rightarrow z_0 \dot{\rightarrow} z_1, a_0 \rightarrow a_0 \dot{\rightarrow} a_1, a_1 \rightarrow z_1 \dot{\rightarrow} z_2$

The Process Hitting modeling



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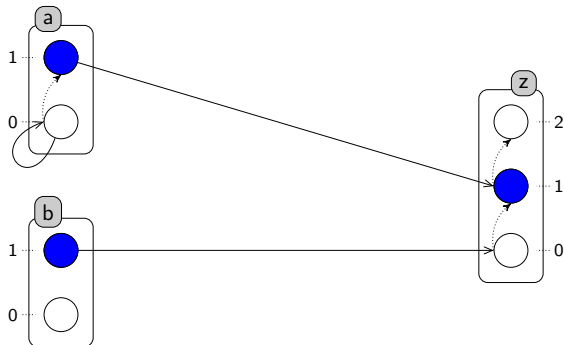
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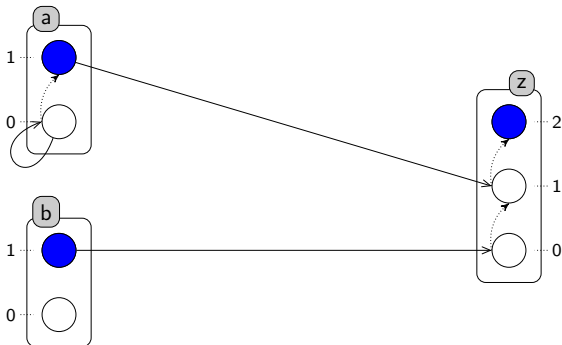
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The Process Hitting modeling



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PH through ASP

Network translation:

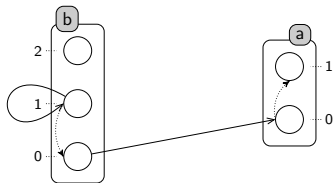
- **Sort:** `sort(A)` .
- **Process:** `process(A,I)` .
- **Action** $a_i \rightarrow b_j \overset{\uparrow}{\vdash} b_k$: `action(A,I,B,J,K)` .

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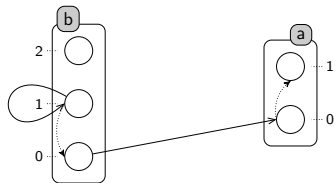


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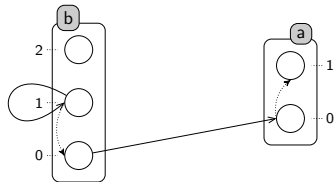
```
process("a", 0..1).
process("b", 0..2).
```


PH through ASP

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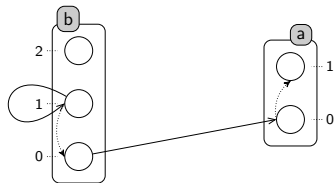
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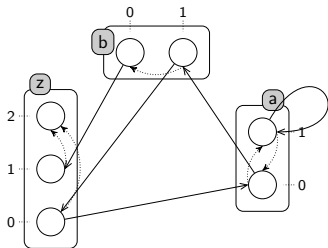
Example :



```
process("a", 0..1).
process("b", 0..2).
sort(X) :- process(X,I).
action("b",0,"a",0,1).
action("b",1,"b",1,0).
```

Fixed Points

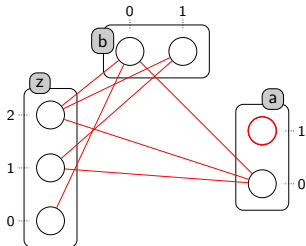
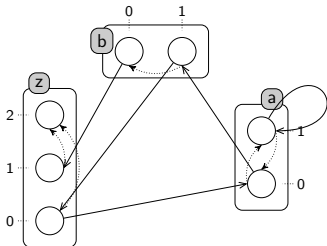
Fixed point = state where no action can be played



Fixed Points

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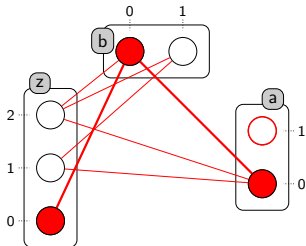
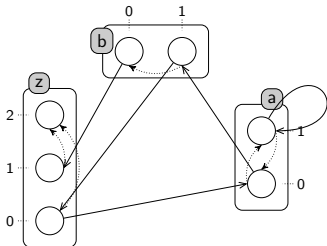
→ Hitless Graph



Fixed Points

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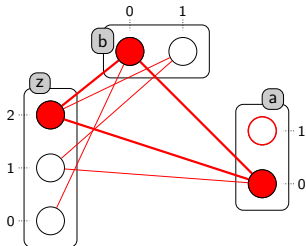
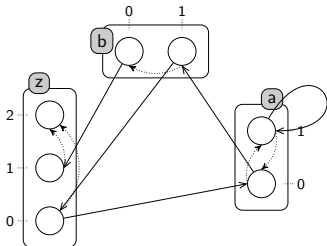
→ Hitless Graph → **n-cliques** = fixed points



Fixed Points

Fixed point = state where no action can be played

→ Hitless Graph → **n-cliques** = fixed points

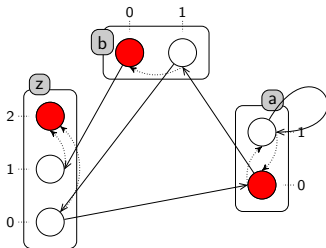


Static analysis

Fixed point through ASP

Implementation:

```
1 {selectProcess(A,I) : shownProcess(A,I) } 1 :- sort(A).
:- hit(A,I,B,J), selectProcess(A,I), selectProcess(B,J), A!=B.
```

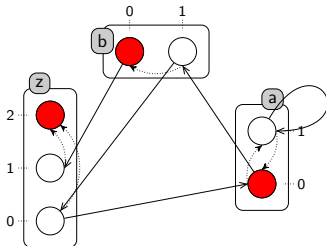


Static analysis

Fixed point through ASP

ASP program result:

Answer 1: `fixProcess(a,0), fixProcess(b,0), fixProcess(z,2).`



Static analysis

Fixed Point

Comparison

Model	#sorts	#states	#fix-point	ASP-PH	PINT-PH
mvbrn	3	12	1	0.000s	0.006s
ERBB	42	2^{70}	3	0.000s	0.017s
tcrsig40	54	2^{73}	1	0.020s	0.021s
tcrsig94	133	2^{194}	0	0.060s	0.027s
egfr104	193	2^{320}	0	0.140s	0.074s

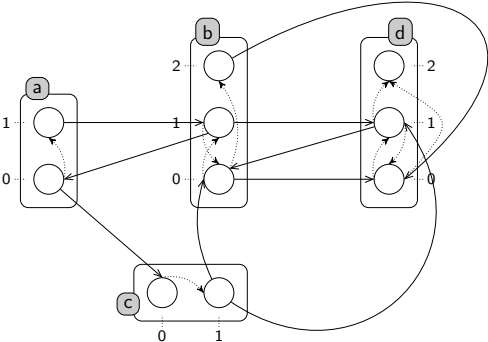
Figure: Execution time of ASP method and PINT applied for biological networks with a desktop computer (core i5 and 4GB RAM).

PINT : a library developed to parse and study PH models.

Dynamic analysis

Reachability

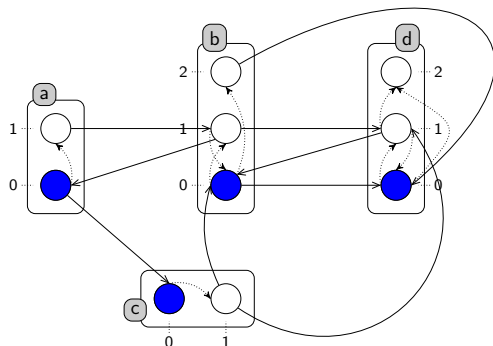
Reachability of processes for PH networks:



Dynamic analysis

Reachability

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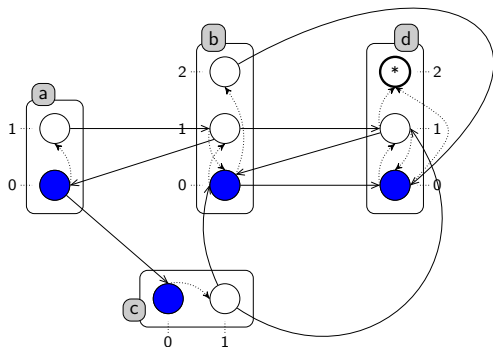
- Initial context

$\langle a_0, b_0, c_0, z_0 \rangle$

Dynamic analysis

Reachability

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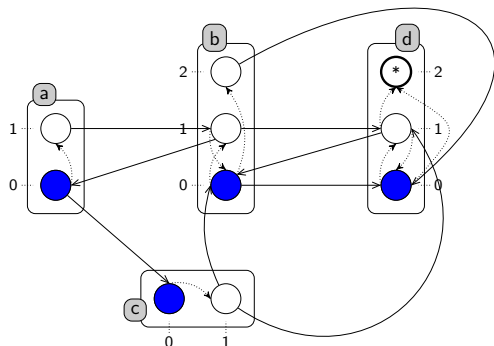
- Objectives

$[\uparrow d_2]$

Dynamic analysis

Reachability

Reachability of processes for PH networks:



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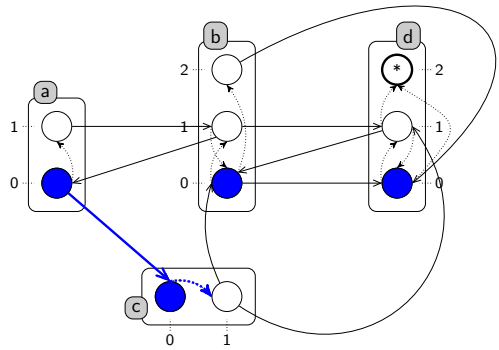
→ Concretization of the objective = scenario

$a_0 \rightarrow c_0 \uparrow c_1 :: b_0 \rightarrow d_0 \uparrow d_1 :: c_1 \rightarrow b_0 \uparrow b_1 :: b_1 \rightarrow d_1 \uparrow d_2$

Dynamic analysis

Reachability

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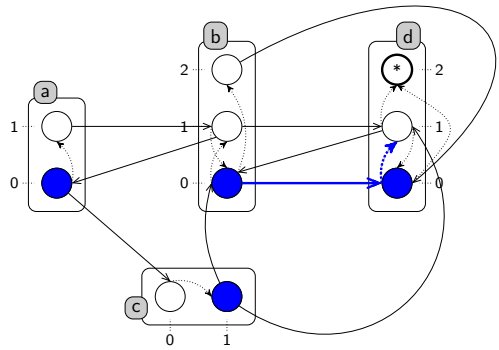
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Dynamic analysis

Reachability

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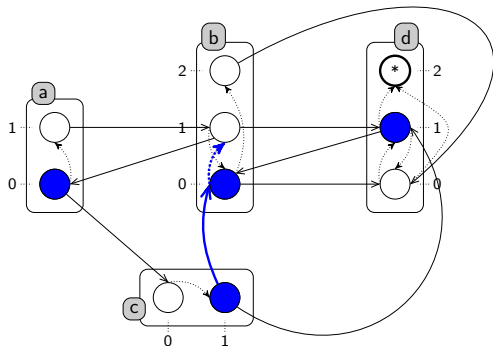
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Dynamic analysis

Reachability

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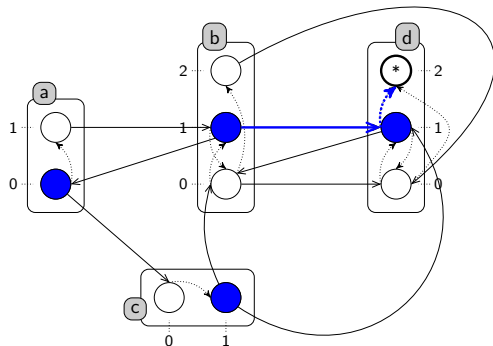
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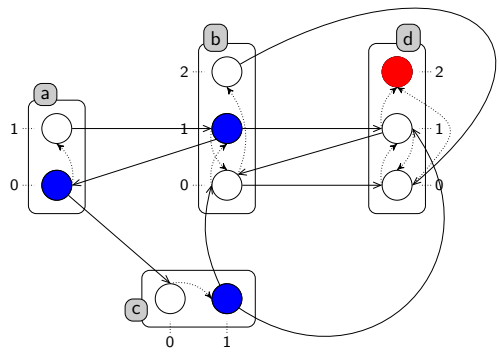
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Dynamic analysis

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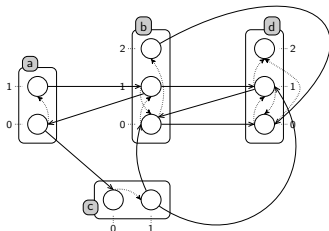
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Dynamic analysis

Evolution through ASP

Network evolution through ASP



Dynamic analysis

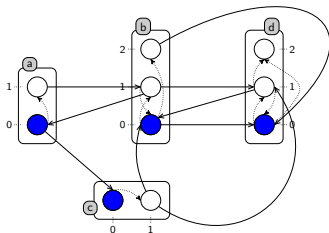
Evolution through ASP

Network evolution through ASP

Initializing :

`init(activeProcess("a",0)).`

avec a: sorte, 0: indice du processus



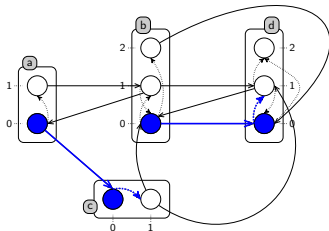
Dynamic analysis

Evolution through ASP

Network evolution through ASP

Playable actions at step T :

```
playableAction(A,I,B,J,K,T) :- action(A,I,B,J,K),
    instate(activeProcess(A,I),T),
    instate(activeProcess(B,J),T), time(T).
```



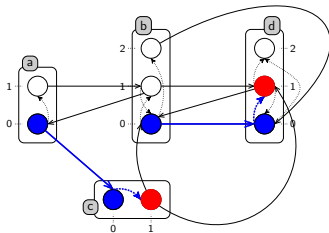
Dynamic analysis

Evolution through ASP

Network evolution through ASP

Change active processes :

```
{activeFromTo(B,J,K,T)} :- playableAction(A,I,B,J,K,T),
                             J!=K, time(T).
                             :- 2{ activeFromTo(B,J,K,T)}, time(T).
```



Dynamic analysis

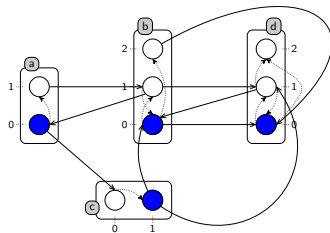
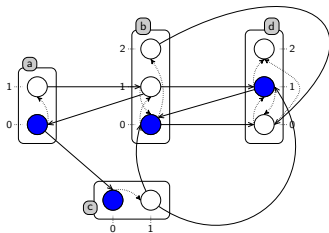
Evolution through ASP

Network evolution through ASP

Active processes at next step ($T+1$) :

```

instate(activeProcess(B,K),T+1) :- activeFromTo(B,J,K,T), time(T).
instate(activeProcess(A,I),T+1) :- instate(activeProcess(A,I),T),
                                     activeFromTo(B,J,K,T), A!=B, time(T).
    
```



Dynamic analysis

Evolution through ASP

Network evolution through ASP

```
time(0..N).
```

Results ($N = 3$) :

```
Answer 1:  activeFromTo("d",0,1,0) activeFromTo("c",0,1,1)
          actifFromTo("b",0,1,2).
```

```
Answer 2:  activeFromTo("d",0,1,0) activeFromTo("b",0,2,1)
```

```
Answer 3:  activeFromTo("c",0,1,0) activeFromTo("d",0,1,1)
          activeFromTo("d",1,0,2) activeFromTo("b",0,1,3)
```

```
...
```

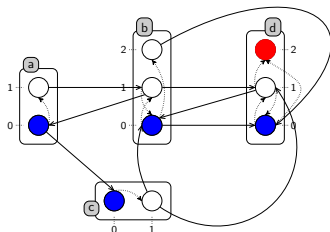
```
Answer 29: activeFromTo("c",0,1,0) activeFromTo("b",0,1,1)
          activeFromTo("a",0,1,2)
```


Dynamic analysis

Reachability through ASP

Success reachability through ASP:

```
goal(activeProcess("d",2)).
```

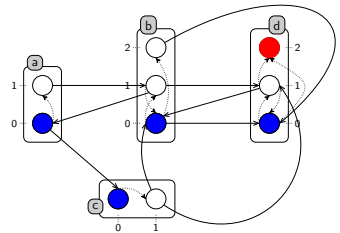


Dynamic analysis

Reachability through ASP

Success reachability through ASP:

```
goal(activeProcess("d",2)).  
satisfiable(F,T) :- goal(F), instate(F,T).  
:- not satisfiableTot.
```

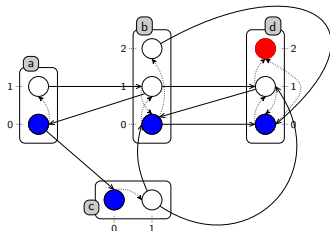


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Reachability through ASP

Success reachability through ASP:

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goal(activeProcess("d",2)).  
satisfiable(F,T) :- goal(F), instate(F,T).  
:- not satisfiableTot.  
time(0..N).
```

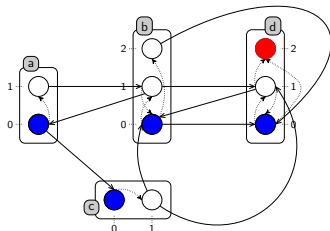


Dynamic analysis

Reachability through ASP

Success reachability through ASP:

```
goal(activeProcess("d",2)).  
satisfiable(F,T) :- goal(F), instate(F,T).  
:- not satisfiableTot.  
time(0..N).  
predict N -> Inconvenient
```



Dynamic analysis

Reachability through ASP

Results for ($N = 2$) :

UNSATISFIABLE

Results for ($N = 3$) :

Answer 1: `activeFromTo(c,0,1,0), activeFromTo(d,0,1,1),
activeFromTo(b,0,1,2), activeFromTo(d,1,2,3).`

Answer 2: `activeFromTo("d",0,1,0) activeFromTo("c",0,1,1)
activeFromTo("b",0,1,2) activeFromTo("d",1,2,3)`

Dynamic analysis

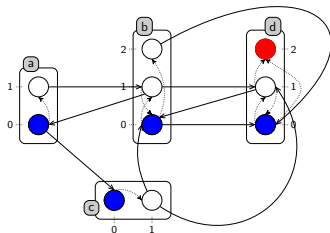
Reachability through ASP

Success reachability through ASP iterative:

```

goal(activeProcess("d",2)).
#base
instate(F,0) :- init(F).
#cumulative t
playableAction(A, I, B, J, K,t), activeFromTo(B, J, K,t),
instate(activeProcess(A, I),t + 1)...
#volatile t
notSatisfiable(t) :- goal(F), not instate(F,t).
:- notSatisfiable(t).

```



Dynamic analysis

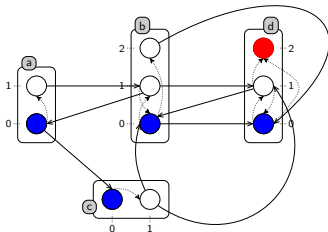
Reachability through ASP

Success reachability through ASP iterative:

Results:

Answer 1: `activeFromTo(c,0,1,0)`, `activeFromTo(d,0,1,1)`,
`activeFromTo(b,0,1,2)`, `activeFromTo(d,1,2,3)`.

Answer 2: `activeFromTo("d",0,1,0)` `activeFromTo("c",0,1,1)`
`activeFromTo("b",0,1,2)` `activeFromTo("d",1,2,3)`



Dynamic analysis

Reachability through ASP

Comparison:

Initializing biological models components and the objectives.

Model-target	#sorts	ASP-TH	PINT	LIBDDD	GINSIM	ASP _I -PH
ERBB-whole	20	0m2.44s	out	1m55.38s	2m31.64s	0m11.84s
ERBB-sub	20	0m2.61s	0m0.03s	1m54.96s	-	0m5.02s
TCR-whole	40	-	Inconc	out	out	4m27.93s
TCR-sub	40	-	0m0.02s	out	-	1m35.08s

Figure: Compared performances of Rocca et al. method denoted by ASP-TH, PINT, LIBDDD, GINSIM and our new iterative method ASP-PH.

General setting of the problem

Limits of discrete modeling

Quantitative information about the delays between two events is abstracted . . . but this information may be crucial in some dynamics.

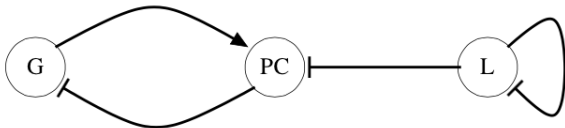
Issues related to the introduction of delays

- Discrete time vs dense time
- How to capture delays in the ASP modeling?

Towards model-checking timed models using ASP

Circadian clock

- Simplified discrete model introduced by (Comet et al., 2012)
- nondeterministic and asynchronous model

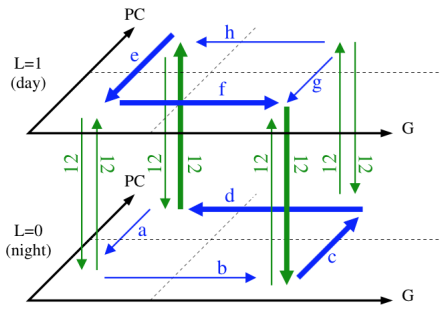


- **PC**: PER-CRY complex
- **G**: set of genes having a positive action on the complex PER-CRY
- **L**: Light

Towards model-checking timed models using ASP

Circadian clock

- Simplified discrete model introduced by (Comet et al., 2012)
- nondeterministic and asynchronous model



Implementation using ASP

Circadian clock

Nodes:

```
process("L",0..1).
process("PC",0..1).
process("G",0..1).
```

Execution time of actions:

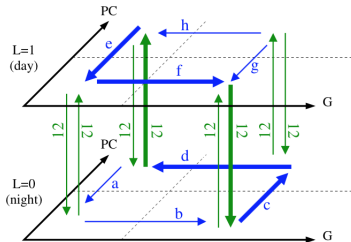
```
equalTo("a",7). equalTo("b",5)...
```

Number of hours for day and night:

```
hoursDay(12). hoursNight(12).
```

Actions:

```
action("G",0, "L",1, "PC",1,0, I):-
equalTo("e",I).
```



Implementation using ASP

Circadian clock

Timer for Light :

`timerL(X,T).`

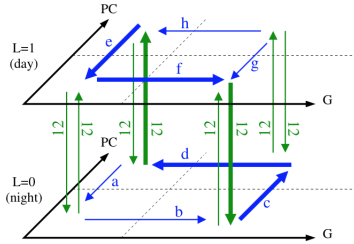
Timer for component now changing :

`timerComp(U,T).`

Reaction is playing or component is changed at T :

`processingActiveFromTo(B,J,K,U, X, T).`

`activeFromTo(B,J,K, T).`



Implementation using ASP

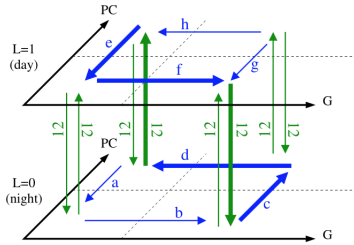
Circadian clock

Result of the evolution of this oscillation after 40 hours:

Answer: 1

```

activeFromTo("PC",0,1,7)
activeFromTo("G",1,0,12)
activeFromTo("PC",1,0,14)
activeFromTo("G",0,1,19)
activeFromTo("PC",0,1,31)
activeFromTo("G",1,0,36)
activeFromTo("PC",1,0,38)
activeFromTo("G",0,1,43)
    
```



Conclusion & Prospects

- New dynamic analysis of Process Hitting models:
 - Fixed point
 - Network evolution
 - Reachability
- Representation of timed automata models through Process Hitting:
Circadian clock
- **Prospects:**
 - Model-checking of for circadian clock
 - Estimation of new action parameters when duration for day/night cycle changes
 - Connecting dynamic properties with resilience
 - Adaptation on other models (PN, Boolean networks, Thomas' models,...)
 - Search of attractors
 - Reverse reachability (*goal* $\rightarrow I_0?$)...

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Thanks for your attention